

ORDRE DES INGÉNIEURS DU QUÉBEC

November 2017 SESSION

Open-book examination  
Calculators : only authorized models  
Duration : 3 hours

16-MK-A2- CIRCUITS

**Question 1 (10 points)**

Find the equivalent resistance between terminals a and b for the circuit of Figure 1.

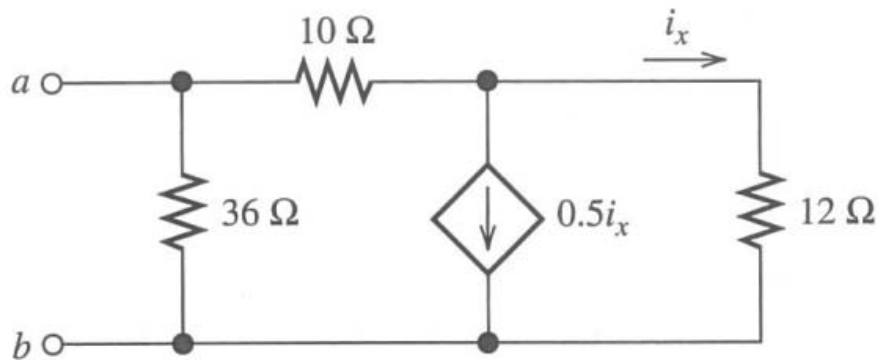


Figure 1

**Question 2 (15 points)**

The variable resistor  $R_0$  in the circuit shown in Figure 2 is adjusted for maximum power transfer to  $R_0$ .

- Find the value of  $R_0$  (10 points).
- Find the maximum power that can be delivered to  $R_0$  (5 points).

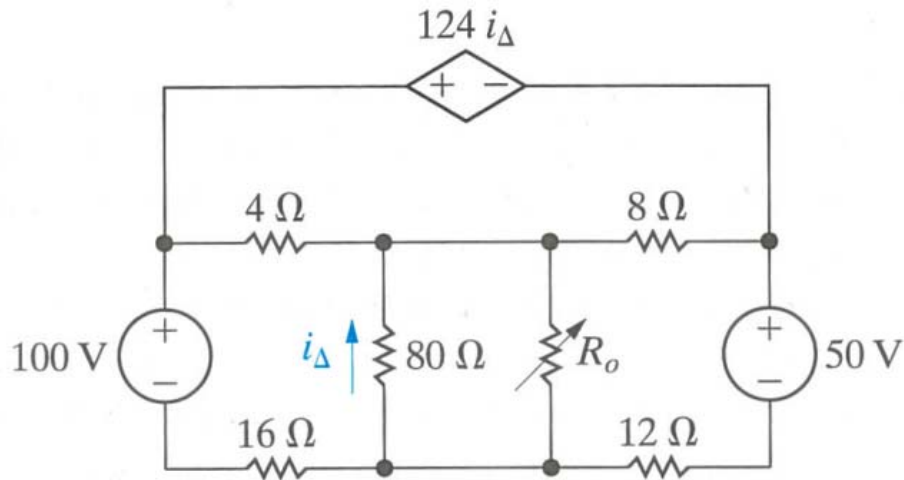


Figure 2

**Question 3 (10 points)**

Consider the circuit shown in in Figure 3 in which  $V_s$  is a DC source Assume that the circuit is in steady state with the switch closed prior to time  $t = 0$  . Find the expression of  $v(t)$  for  $t \geq 0$ .

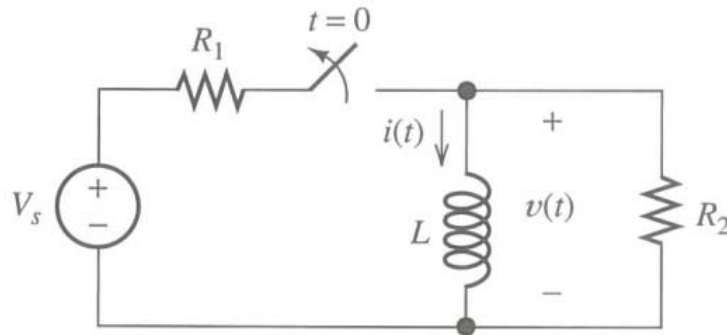


Figure 3

**Question 4 (15 points)**

Consider the circuit shown in Figure 4 with  $R = 500\ \Omega$ ,  $L = 10\ \mu\text{H}$  et  $C = 1000\ \text{pF}$ .

- Find the undamped resonant frequency, the damping coefficient, and the damping ratio (5 points).
- The initial conditions are  $v(0^+) = 0$  and  $i_L(0^+) = 0$ . Show that this requires that  $\left.\frac{dv}{dt}\right|_{t=0^+} = 10^9\ \text{Vs}^{-1}$  (5 points).
- Find the general solution  $v(t)$  (5 points).

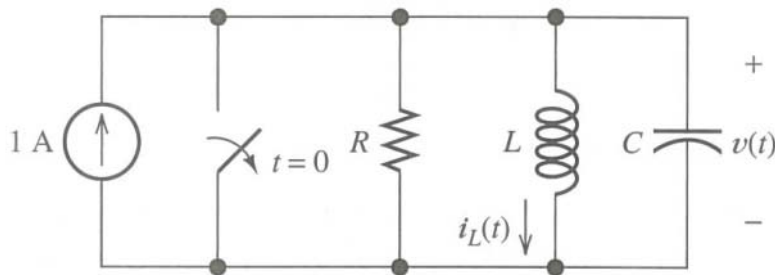


Figure 4

**Question 5 (10 points)**

Find the impedance  $Z_{ab}$  in the circuit shown in Figure 5. Express  $Z_{ab}$  in both polar and rectangular form.

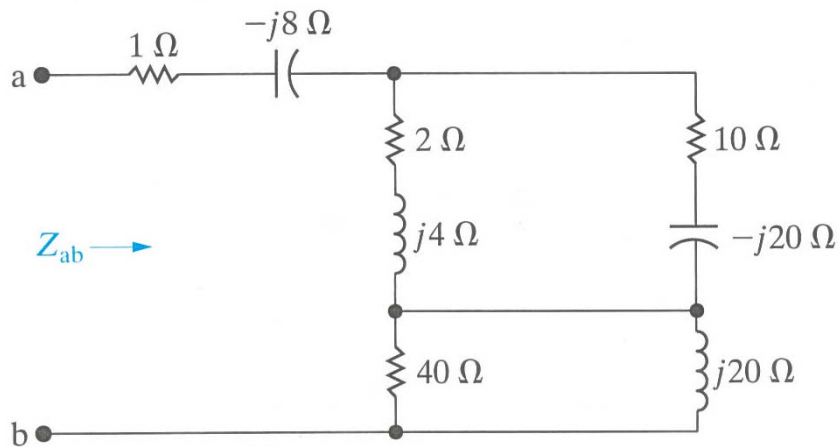


Figure 5

### Question 6 (20 points)

The variable resistor  $R_0$  in the circuit shown in Figure 6 is adjusted until maximum average power is delivered to  $R_0$ .

- Find the value of  $R_0$  (5 points).
- Calculate the average power delivered to  $R_0$  (5 points).
- If  $R_0$  is replaced with a variable impedance  $Z_0$ , what is the maximum average power that can be delivered to  $Z_0$  (5 points)?
- In case c), what percentage of the circuit's developed power is delivered to  $Z_0$  (5 points)?

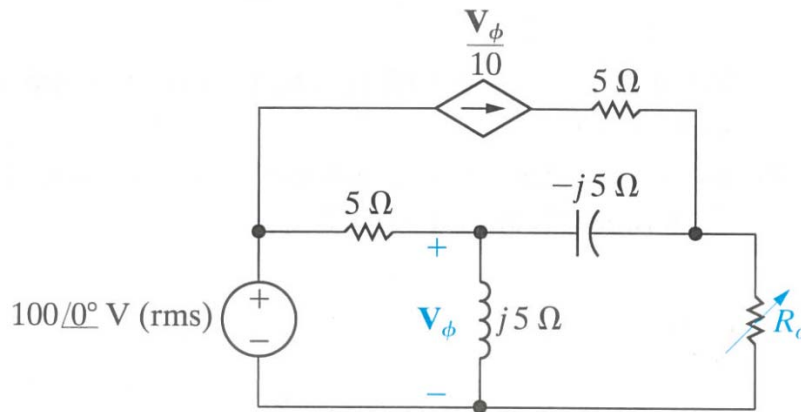


Figure 6

### Question 7 (20 points)

The operational amplifier in the circuit shown in Figure 7 is considered ideal. Calculate the average power delivered to the 1 kΩ resistor when  $v_g = \cos 1000t$  V.

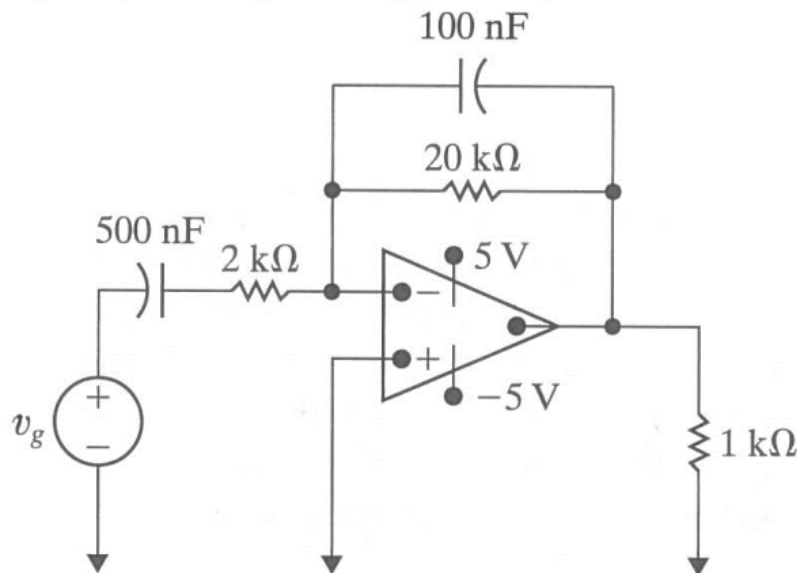


Figure 7