

ORDRE DES INGÉNIEURS DU QUÉBEC

May 2015 SESSION

Open-book examination

Non-programmable calculators: only authorized models

Duration : 3 hours

**14-IN-A5 Quality planning, control and assurance**

**QUESTION #1 (8 points)**

The fraction of nonconforming product manufactured by a company is 99.9945%. Can we say that the company is Six Sigma? Justify your answer quantitatively.

**QUESTION #2 (14 points)**

- a) On a production line, an automatic process eliminates the pieces having a length of less than 9 cm or greater than 11 cm. Knowing that the length of the parts is normally distributed with a mean of 10 cm and a standard deviation of 0.4 cm, how many parts have to be produced to get 1000 good parts? (10 pts)
- b) MicroTek manufactures switches with indicator lights. According to the test results accumulated in recent months, the fraction of nonconforming switches is 10%. We take, randomly from the production, 12 switches to inspect them. What are the chances in percentage, to observe exactly four nonconforming switches? (4 pts)

**QUESTION #3 (25 points)**

Control charts for  $\bar{X}$  and  $R$  are maintained on a process. After 20 preliminary subgroups each of size 3 are evaluated, you have the following data:

$$\sum_{i=1}^{20} \bar{x}_i = 5502 \quad \text{and} \quad \sum_{i=1}^{20} R_i = 60$$

- a) Set-up the control charts using these data (6 pts).
- b) Assume that the process exhibits statistical control. Estimate the process mean and standard deviation (4 pts).
- c) Suppose that the quality characteristic is normally distributed with specification at  $275 \pm 6$ . Estimate the fraction nonconforming produced by this process (8 pts).
- d) How much reduction in process variability would be required to make this a Six Sigma process? (7 pts)

**QUESTION #4 (17 points)**

A control chart is used to control a plastic part manufactured in an injection molding process. Ten subgroups yield the data in table 1.

**Table 1: Data for question #4**

Sample Number	Sample Size	Number nonconforming
1	100	10
2	100	15
3	100	31
4	100	18
5	100	24
6	100	12
7	100	23
8	100	15
9	100	8
10	100	8

- a) Set-up an appropriate control chart for this process (8 pts)
- b) Is the process in statistical control? Justify your answer. (5 pts)
- c) What center line and control limits should be used for controlling future production? (4 pts)

**QUESTION #5 (20 points)**

The molecular weight of a particular polymer should fall between 2100 and 2350. Fifteen samples of this material were analyzed. The results are presented in table 2. Assume the molecular weight is normally distributed.

**Table 2: data for question #5**

2232	2305	2169	2404	2304
2251	2369	2326	2295	2272
2153	2304	2283	2259	2241

- a) Estimate the potential capability of the process and interpret this ratio (4 pts)
- b) Estimate the actual process capability and interpret this ratio (10 pts)
- c) Compare the potential and actual ratios. What do you conclude? (6 pts)

**QUESTION #6 (16 points)**

A company wants to design a single-sampling plan such that the probability of acceptance is 95% for lots with fraction defective of 1% and the probability of acceptance is 10% for lots with defective of 8%. A consultant suggests the following single-sampling plan:  $n = 75$ ,  $c = 1$ .

Does the company should use this plan? Does the plan meet the desired probabilities? Use the operating-characteristic curve to justify your answer quantitatively.